

You will be graded on your COMMUNICATION of physics understanding

#1 You and your friends are excited to take part in the X-treme skate board challenge: Two skate boarders drop off opposite (rounded) sides of a (dry) swimming pool and stick to each other at the bottom of the pool! On the left side, a skater drops from  $H_0$ , while another skater with twice the mass drops from half the height from the right side. They collide in the middle.

- After the collision, (joined together) which way are they going, or are they at rest? Of course, you know to provide a thorough explanation.
- The left side skater is 50 kg and drops from 6 m, while the right side skater is 100 kg and drops from 3 m. Calculate the approximate final velocity of the two bodies stuck together.

Energy lens  $E_g \Rightarrow E_k$

$$E_p = E_k$$

$$mgh = \frac{1}{2}mv^2$$

$$v = \sqrt{2gh}$$

$$v_L = \sqrt{2gh_0}$$

$$v_R = \frac{1}{\sqrt{2}} v_L$$

$\vec{p}$  lens  $\vec{p}$  is conserved,

$F_{\text{outside}} \approx 0$

$$\vec{p}_L = m_L \vec{v}_L$$

$$\vec{p}_R = m_R \vec{v}_R$$

$$p_L = m_0 v_L$$

$$p_R = 2m_0 \frac{1}{\sqrt{2}} v_L = \frac{2}{\sqrt{2}} m_0 v_L = \sqrt{2} m_0 v_L$$

$$p_R = \sqrt{2} p_L \approx 1.4 p_L$$

$$\sum \vec{p}_i = \sum \vec{p}_f$$

$$-p_L + p_R = m_f v_f$$

$$m_f v_f = p_R - p_L$$

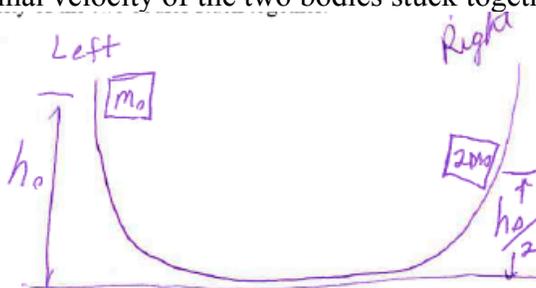
$$= \sqrt{2} p_L - p_L$$

$$= (\sqrt{2} - 1) p_L$$

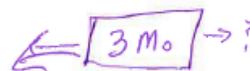
$$3 m_0 v_f = (0.41) m_0 (2gh_0)^{\frac{1}{2}} \quad h_0 = 6 \text{ m}$$

$$v_f = \frac{1}{3} (0.41) (2 \cdot 10 \text{ m/s}^2 \cdot 6 \text{ m})^{\frac{1}{2}}$$

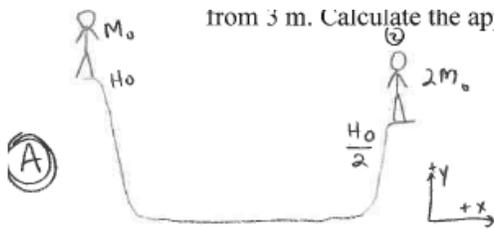
$$= 0.133 (11) \frac{\text{m}}{\text{s}} \approx \underline{\underline{1.4 \text{ m/s}}}$$



← +



from 3 m. Calculate the approximate final velocity of the two bodies stuck together.



energy less because it changes forms  
 momentum less because it is conserved  
 because of the minimal outside forces  
 (inelastic)

- KE not conserved

While KE isn't conserved, the PE of each must equal KE at the bottom

$$mgh_0 = \frac{1}{2}mv^2$$

$$2mgh_0 = \frac{1}{2}mv^2$$

$$m_0 v_1 + (-v_2 m_2) = 3m v_f$$

$$m_0 \sqrt{2gh_0} - 2m_0 \sqrt{gh} = 3m_0 v_f$$

$$\sqrt{2gh_0} = v_1$$

$$-\sqrt{gh} = v_2$$

$$\frac{\sqrt{2gh_0}}{3kg} - \frac{2\sqrt{gh}}{3kg} = v_f$$

$$\sum \vec{p}_i = \sum \vec{p}_f$$

the momentum of the second skateboarder is larger and negative, so the final velocity is negative. They are going left after colliding

A+

$$\textcircled{B} \quad (50 \text{ kg}) \sqrt{2 \cdot 10 \text{ m/s}^2 \cdot 6 \text{ m}} - (100 \text{ kg}) \sqrt{10 \text{ m/s}^2 \cdot 6 \text{ m}} = 150 \text{ kg } v_f$$

$$\approx 50 \text{ kg} \cdot \sqrt{120 \text{ m}^2/\text{s}^2} - 100 \text{ kg} \sqrt{60 \text{ m}^2/\text{s}^2} = 150 \text{ kg } v_f$$

$$\approx \frac{50 \cdot 11 \text{ kg m/s}}{50 \cdot 3 \text{ kg}} - \frac{100 \cdot 8 \text{ kg m/s}}{100 \cdot 1.5 \text{ kg}} = \frac{150 \text{ kg } v_f}{150 \text{ kg}}$$

$$\hat{=} 3 \text{ m/s} - 5 \text{ m/s} = v_f$$

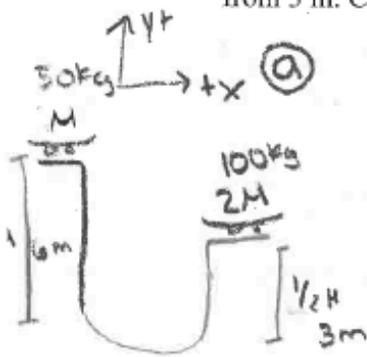
$$v_f = -2 \text{ m/s}$$

closer to 4 m/s

!!!

This is great work!  
 I love the estimating

from 3 m. Calculate the approximate final velocity of the two bodies stuck together.



ENERGY LENS

$$PE = KE$$

$$mgh = \frac{1}{2}mv^2$$

$$gh = \frac{1}{2}v^2$$

$$2gh = v^2$$

$$v = \sqrt{2gh}$$

$$Mgh = \frac{1}{2}Mv^2$$

$$\frac{1}{2}Mg = \frac{1}{2}v^2$$

$$Hg = v^2$$

$$v = \sqrt{gH}$$

MOMENTUM LENS

$$m_1v_1 = m_2v_2$$

$$M\sqrt{2gH} - 2M\sqrt{gH} = 3Mv$$

$$v = \frac{M\sqrt{2gH} - 2M\sqrt{gH}}{3M}$$

$2M\sqrt{gH} > M\sqrt{2gH}$   
therefore numerator is negative  
negative divided by a positive  
is negative

⊖ answer moving to the left

547.7

because?

A

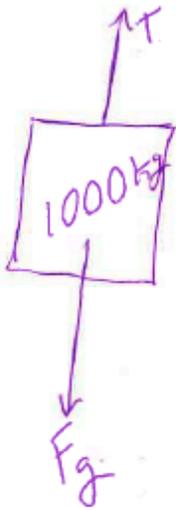
$$\textcircled{b} v_f = \frac{M\sqrt{2gH} - 2M\sqrt{gH}}{3M}$$

$$v_f = \frac{50\text{kg}\sqrt{2(10\text{m/s}^2)(6\text{m})} - 100\text{kg}\sqrt{(10\text{m/s}^2)(6\text{m})}}{150\text{kg}}$$

$$v_f = 1.51 \text{ m/s to the left}$$

nice work...  
good units!  
well organized

#2 Your friend is standing in a 1000 kg elevator (combined mass). At a height of 20 m, she's moving downward at 8 m/s. She continues at this speed for 1 second and then smoothly comes to rest at some height over the next 2 s. Please make the graphs describing her motion and the tension in the elevator cable during this experience. Label the axis to make the values explicitly clear. **A lot of students made sign errors. I think you should decide which way is positive and check it for all calculations. Also, state your lens(es).**



Kinematics  
 $v$  as  $f(\text{time})$

$a = \frac{\Delta v}{\Delta t} = \frac{8 \text{ m/s}}{2 \text{ s}} = 4 \text{ m/s}^2$   
 $v = \frac{\Delta x}{\Delta t} \quad \Delta x = v \Delta t$

Dynamics lens.  $F$  cause  $a$

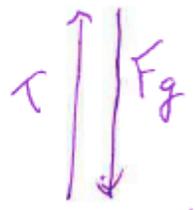
$\sum \vec{F} = m\vec{a}$

$T + F_g = m\vec{a}$

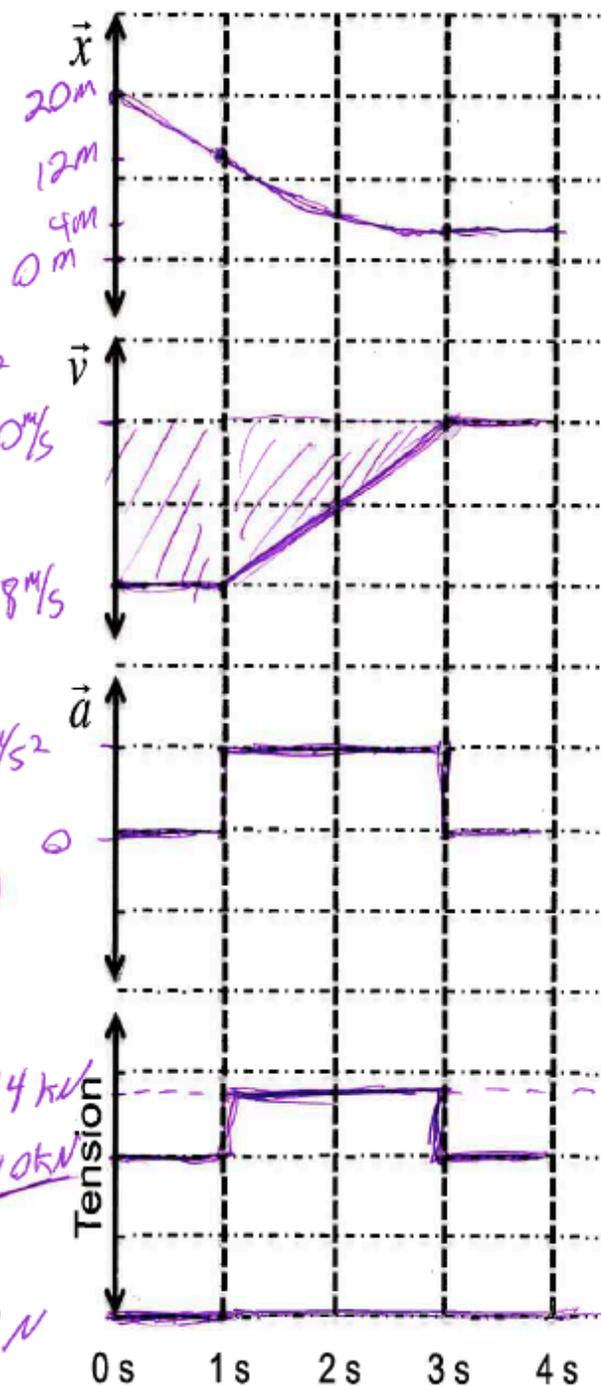
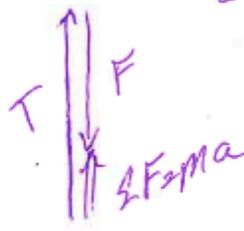
$T = F_g + ma$

$a = 0$

$T = F_g = mg = 1000 \text{ kg} \cdot 10 \text{ m/s}^2 = 10 \text{ kN}$



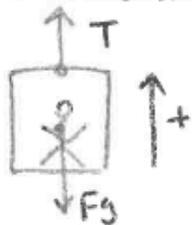
$a = 4 \text{ m/s}^2$



$T = 10 \text{ kN} + 1000 \text{ kg} (4 \text{ m/s}^2)$   
 $10 \text{ kN} + 4 \text{ kN} = 14 \text{ kN}$

Label the axis to make the values explicitly clear.

Lens: Kinematics:  $x$  and  $\vec{v}$  given as explicit fn of time.



$$x = \int v dt$$

$$t = 0 \text{ to } 1 \text{ s} \\ x = 8 \text{ m/s} (1 \text{ s}) \\ x = 8 \text{ m}$$

$$t = 1 \text{ to } 3 \text{ s} \\ x = 8 \text{ m/s} (2 \text{ s}) (\frac{1}{2}) \\ x = 8 \text{ m}$$

$v = 8 \text{ m/s}$  at  $t = 0 \text{ s}$  to  $t = 1 \text{ s}$   
Comes to rest, velocity goes to 0 over 2 s.

$$a = \frac{\Delta v}{\Delta t}$$

$$\Delta v = 0 \text{ m/s} - (-8 \text{ m/s}) \\ = +8 \text{ m/s}$$

$$\Delta t = 2 \text{ s}$$

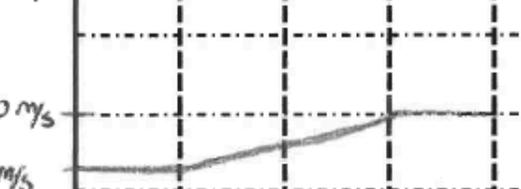
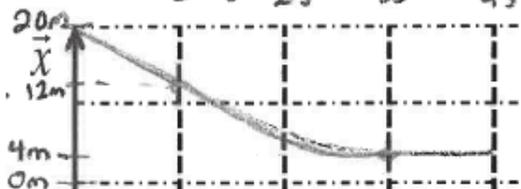
$$= \frac{8 \text{ m/s}}{2 \text{ s}} = 4 \text{ m/s}^2$$

$\vec{a}$  is  $\frac{\Delta v}{\Delta t}$ .  $v$  changes  $8 \text{ m}$  in  $2 \text{ s}$

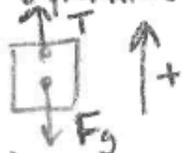
$\vec{a}$  is constant

$\vec{a}$  is zero 0 to 1 s and 3 to 4 s

$t = 1 \text{ s}$     $2 \text{ s}$     $3 \text{ s}$     $4 \text{ s}$



Lens: Dynamics:  $\vec{a}$  caused by forces:



tension and  $F_g$  14,000 N

$$\Sigma \vec{F} = m\vec{a}$$

When  $\vec{a} = 0 \text{ m/s}^2$

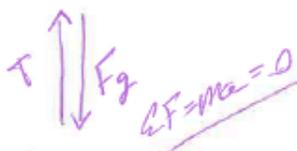
$$\Sigma \vec{F} = 0 = T + F_g$$

$$T = F_g$$

$$T = mg$$

$$= (1000 \text{ kg})(10 \text{ m/s}^2)$$

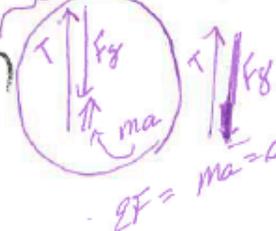
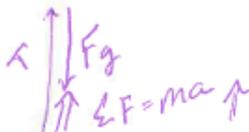
$$T = 10,000 \text{ N}$$



When  $\vec{a} = 4 \text{ m/s}^2$

$$1000 \text{ kg}(4 \text{ m/s}^2) = T + (1000 \text{ kg})(-10 \text{ m/s}^2)$$

$$T = 14,000 \text{ N}$$



#3 I have a 2 kg block, bouncing between two springs as shown below. Each spring is about 1 m long and there is a 2 m low friction track in between. The spring on the left has a spring constant twice as large as that on the right:  $k_L = 2k_R$ .

- I compress the spring on the left and use it to launch the mass across the low friction floor into the spring on the right. How far does the right spring compress? That is:  $\Delta x_R = ?? \Delta x_L$ . Show work.
- Above the image below, please make a potential energy diagram, showing the potential energy of the block as a function of displacement. I'm just looking for the shape. You can't put scales on the axis because I don't give you the required constants.

For (c) and (d) below, what if the floor is not frictionless? What if there is a 2 m section of floor that has a coefficient of friction of 0.3 with the block?

- Find the acceleration of the block on this surface as it slides to the right after leaving the spring.
- How would this friction change the calculation you did for (a) above? How would you go about finding the compression in the second spring now? Please explain and set up the equation(s) necessary. There is not enough information to calculate the value.

$$E_{SL} \Rightarrow E_K = E_{SR}$$

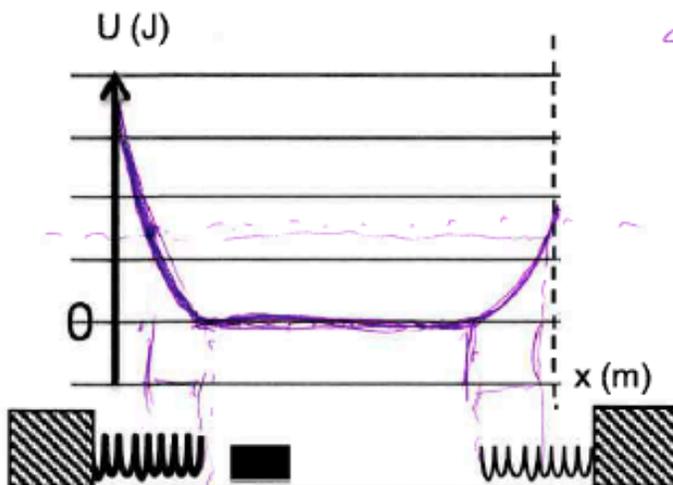
$$\frac{1}{2} k_L x_L^2 = \frac{1}{2} k_R x_R^2 \quad x_R^2 = 2 x_L^2$$

$$x_R = \sqrt{2} x_L \quad \leftarrow 1.4 x_L$$

c) Dynamics  $F_f \Rightarrow a$

$\sum \vec{F} = m\vec{a}$

$F_f = \mu N = ma$

$$a = \frac{\mu N}{m} = \frac{\mu mg}{m} = \mu g = 3 \text{ m/s}^2$$


d) Energy  $E_{SL} \Rightarrow E_{SR} + \text{Heat}$

$$\text{Heat} = \int F_f dx = F_f \Delta x$$

$$= \mu mg \Delta x$$

$$= .3(20N) \cdot 2m$$

$$= 12J$$

a) lens: energy b/c if the floor is frictionless, no energy is lost to thermal energy, so the potential in spring transfers completely to kinetic after the spring expands & returns to spring potential energy as it hits the right spring. and in this closed system the total energy is conserved

$E_{spL} \rightarrow E_k \rightarrow E_{spR} \rightarrow E_k \dots$  (cont. as it goes back & forth)

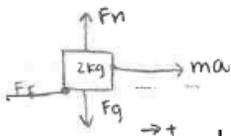
$E_{sp} = \frac{1}{2}k\Delta x^2$  &  $E_k = \frac{1}{2}mv^2$  &  $E_{sp} = E_k$

The left- & right spring produce the same amount of  $E_p$  (b/c conservation of energy) so  $E_{spL} = E_{spR}$  &  $k_L = 2k_R$ . In order to cancel out the doubled  $k$  value (to make the potential energy be the same) you need to make  $\Delta x^2 = 2$ , so:

$\Delta x_R = \sqrt{2} \Delta x_L$   $\hookrightarrow \frac{1}{2}(2k_R)\Delta x_R^2 = \frac{1}{2}k_L \Delta x_L^2$

\*\* If the floor wasn't frictionless ( $\mu = .3$ ) then the potential energy would ~~not~~ all transform to kinetic energy ( $E_{sp} \neq E_k$ ), instead the friction would cause the block to lose kinetic energy as it bounces back & forth

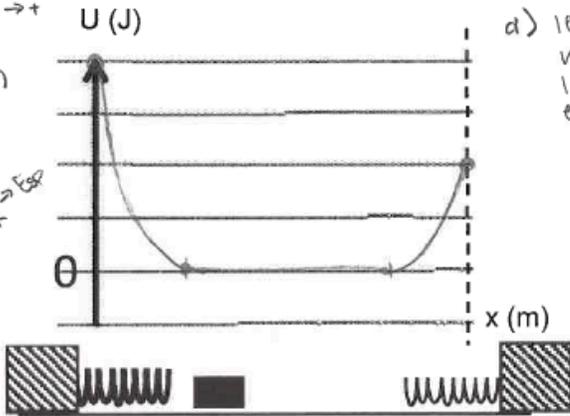
c) lens: dynamics b/c forces cause acceleration & the force of friction goes "against" relative velocity of block



\*  $F_g = F_n$  b/c no up/downwards acceleration

$F_f = \mu F_n$  &  $F_n = F_g = mg$  &  $\mu = .3$  &  $\Sigma F = ma$  &  
 $F_f = ma \rightarrow \mu mg = ma \rightarrow a = \mu g$   
 $a = (.3)(10m/s^2) = 3m/s^2$

b) energy lens  $E_{sp} \rightarrow E_k \rightarrow E_{sp}$



d) lens: energy b/c potential energy wouldn't all go to kinetic energy, instead, it would be kinetic & thermal energy

$E_{sp} \rightarrow E_k + E_{th} \rightarrow E_{sp} \dots$

as the block bounces back & forth, thermal energy would increase & spring energy would decrease (so  $\Delta x$  would also decrease)

$E_{sp} = \frac{1}{2}k\Delta x^2$  &  $E_k = \frac{1}{2}mv^2$  &  $E_{th} = W$  by friction

$E_{sp} = E_k + E_{th}$   
 $\frac{1}{2}k\Delta x^2 = \frac{1}{2}mv^2 + \mu F_n x$   
 $\quad \quad \quad = \frac{1}{2}k\Delta x^2 + \mu F_n x$

$W = F_f x$   
 $W = \mu F_n x$   
 $=$

#4 Your 100 kg friend, said he ran up a flight of stairs in 4 seconds... starting from rest and still going strong at the end! You measure the stairs and note that the flight is 20 m long and rises 5 meters.

Estimate your friend's power output. State any assumptions you make in the process. **There need to be considerations for both kinetic and potential energy for full credit. You should state the assumptions (simplification) you make for the motion.**

$$P = \frac{W}{t} = \frac{\Delta E}{\Delta t}$$

~~$E_p = E_k$~~   
 $W \Rightarrow E_p + E_k$

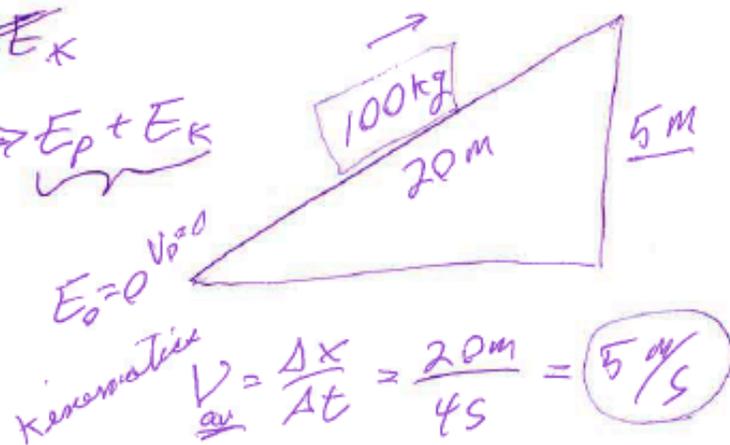
$$\Delta E = E_p + E_k$$

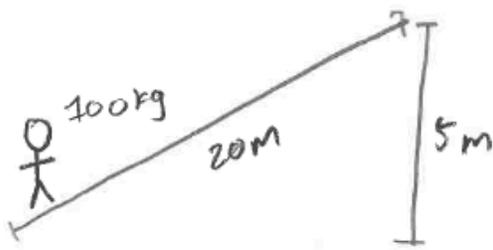
$$= mgh + \frac{1}{2}mv^2$$

$$= 100\text{kg} \cdot 10\text{m/s}^2 \cdot 5\text{m} + \frac{1}{2}(100\text{kg})(5\text{m/s})^2$$

$$= 5000 \text{ kg} \frac{\text{m}^2}{\text{s}^2} + 1250 \text{ kg} \frac{\text{m}^2}{\text{s}^2} = \underline{6250\text{J}}$$

$$P = \frac{\Delta E}{\Delta t} = \frac{6250\text{J}}{4\text{s}} \approx 1.6 \text{ kW} \approx \underline{2\text{Hp}}$$





$$t = 4s$$

$$KE = 0$$

We find power using the energy lens as it is the change of energy over time. We analyze both potential and kinetic energy.

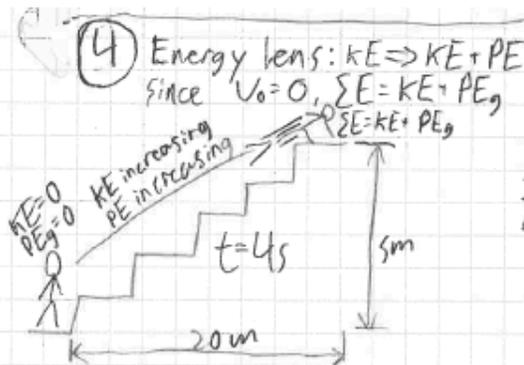
Potential energy can be found with  $PE = mgh$ . The initial potential energy is 0 because the height is 0. The final potential energy  $PE = 100\text{kg} \cdot 10\text{m/s}^2 \cdot 5\text{m} = 5000\text{J}$ , so a 5000J change in PE.

This change occurs over 4 seconds, so power =  $dE/dt = 5000\text{J}/4\text{s} = 1250\text{W}$ .

Because the person starts from rest, there is a change in KE from the bottom to top of the stairs. The initial KE is 0. We use kinematics to find the velocity, which we will then use to find the final kinetic energy.  $v = \Delta x / \Delta t = 20\text{m total} / 4\text{seconds} = 5\text{m/s}$  velocity at the top. We then find  $KE = 1/2 mv^2 = 1/2 (100\text{kg})(5\text{m/s})^2 = 1250\text{J}$ . The total change in KE = 1250J. This also occurs over 4 seconds, so power =  $1250\text{J}/4\text{s} = 312.5\text{W}$ .

The total power is the sum of  $1250\text{W} + 312.5\text{W}$ , so a total of  $1562.5\text{W}$ .

--- OR ---



④ Energy lens:  $KE \Rightarrow KE + PE$

Since  $v_0 = 0$ ,  $\Sigma E = KE + PE_g$

All energy is conserved, the ATP in her body is converted through work to KE and  $PE_g$

$$W = F \Delta x = \Delta E \quad \Delta E = (KE_f + PE_f) - (KE_i + PE_i) > 0$$

$$\Delta E = \frac{1}{2}mv^2 + mgh$$

In order to find  $v$  we use kinematics lens, position as a function of time.  $v = \frac{\Delta x}{\Delta t} = \frac{20\text{m}}{4\text{s}} = 5\text{m/s}$

$$\begin{aligned} W = \Delta E &= \frac{1}{2}mv^2 + mgh \\ &= \frac{1}{2}(100\text{kg})(5\text{m/s})^2 + (100\text{kg})(10\text{m/s}^2)(5\text{m}) \\ &= 1250\text{J} + 5000\text{J} \\ &= 6250\text{J} \end{aligned}$$

$$\text{Power} = \frac{W}{\Delta t} \Rightarrow w = 6250\text{J}$$

$$= \frac{6250\text{J}}{4\text{s}} = 1562.5\text{W} \approx 1.6\text{kw}$$