

Schwartz Problem Set #7

- 1) Say you live in Alaska where it's routinely $-40\text{ }^{\circ}\text{C}$ for days on end. You want to keep your house at $25\text{ }^{\circ}\text{C}$ and you presently burn natural gas with an efficiency of about 85% (some heat remains in the exhaust in order to not condense the water vapor). However, you're considering using (NGCC) electricity to heat your house with a heat pump. You're happy that there's a narrow but deep ocean inlet next to your house that never freezes all winter long!
 - a) Why are you happy to have this ocean inlet?
 - b) Draw a picture describing how this heat pump would work. Include all mechanisms and the house and area as well.
 - c) Estimate the ideal coefficient of performance for heating your house using the ocean inlet.
 - d) In order to drive the heat to the evaporator coils from the water, you need $10\text{ }^{\circ}\text{C}$ difference and you need $15\text{ }^{\circ}\text{C}$ difference between the condenser coils and the room to drive heat into the room. NOW what is the best coefficient of performance you would get?

- 2) You don't ever get your ideal COP for a heat pump for the same reason that we don't have heat engines achieving the Carnot Thermodynamic Limit. We practically can't perfectly operate (for instance) a perfect isothermic process if we're in a hurry to get things done. A reasonable COP for such a cold place might be about 4. Please compare the following three technologies:
 - a) Burning natural gas whereby you extract about 85% of the chemical potential energy from the natural gas.
 - b) Using an electric heater in your house. Electric heaters are all 100% efficient (despite what advertisements might say along the lines of "high efficiency"). All the electricity turns to thermal energy.
 - c) Using an electric heat pump.

For the above three scenarios, please compare how much you would spend to heat your house, and how much CO_2 would be emitted. Let's see... you need something to compare it to? Using a space heater, you would use 1000 kWh per month. In Alaska, they pay about $\$0.16/\text{kWh}$ just like us. So, given these two numbers, please calculate the costs and CO_2 emissions (kg of CO_2/month) for all three scenarios.

- 3) You build a wind turbine for Dong! The next generation. Remember the last slide in Friday's lecture?: So take a look at the present size... yes, the radius is close to a football field in length. OK, now double it. And out in the North Sea, you expect to gather electricity at winds all the way up to 15 m/s !
 - a) Calculate the amount of power one of these turbines will put out in 15 m/s wind, if we are able to achieve the Betz Limit.
 - b) You can't really achieve the Betz Limit. How close will you come? Are we "pretty close" to the Betz Limit?

