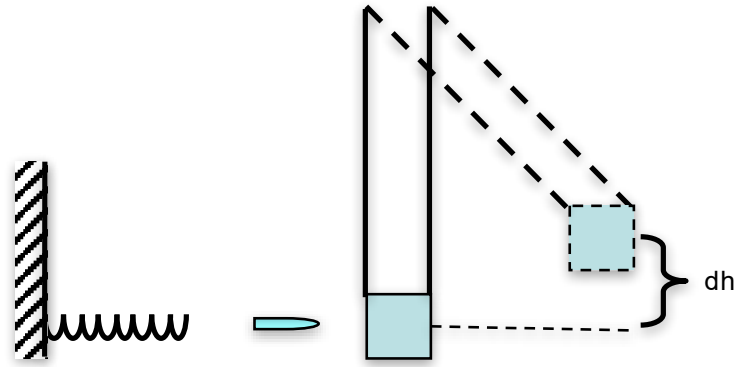


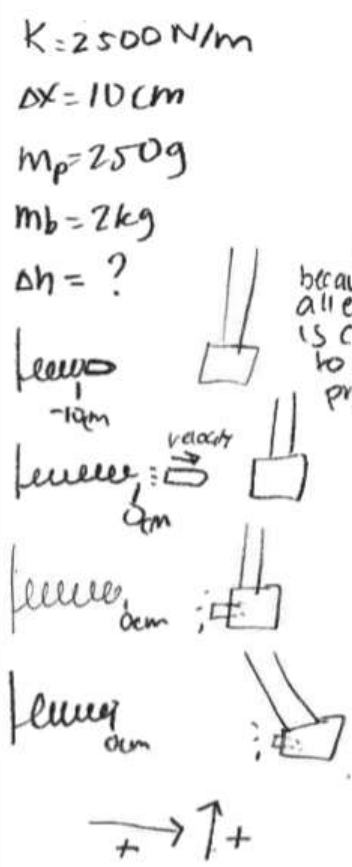
1. A spring of spring constant 2500 N/m is compressed 10 cm behind a 250 g projectile. When released, the projectile is fired into and sticks inside of a 2.0 kg block. The block and projectile lift up to a maximum height  $dh$ . I want to find  $dh$ . I have a plan to use  $U_{sp} = U_g$  to solve for the final height. Does this method work?

- If this the correct way to find  $dh$ , please explain why this is correct, and find  $dh$ .
- If this method doesn't work, please explain why it will not work and what has to be done differently to find  $dh$ . You don't have to calculate it.



Use as much paper as you like. Your work is important for us to read!

Below, please see two solutions... one is clear with large writing. However, the second is my favorite because of the reflection indicating, "I did this wrong" and then they did it correctly.



$K = 2500 \text{ N/m}$   
 $\Delta x = 10 \text{ cm}$   
 $m_p = 250 \text{ g}$   
 $m_b = 2 \text{ kg}$   
 $dh = ?$

This does not work. If you use an energy lens, the  $U_{sp} = KE_{\text{initial}}$  of the projectile as it is released from the spring. Once it hits the block, a lot of the energy is converted into heat energy as well as the KE of the system so the total energy, which came from the  $U_{sp}$  actually equals  $KE_{\text{system}} + \text{Heat energy}$ . Then the KE left is converted to  $U_g$ , but not all the energy of the system will be.

Instead, you should use an energy lens to find the KE of the projectile before it hits the block which is equal to  $U_{sp}$ , because all the  $U_{sp}$  is converted to KE and there is no other energy source and then use a momentum lens to find the velocity of the block and projectile as one after the collision, because momentum is conserved since there are no other outside forces affecting the system that will affect the collision. then use that velocity to find the KE

Name \_\_\_\_\_

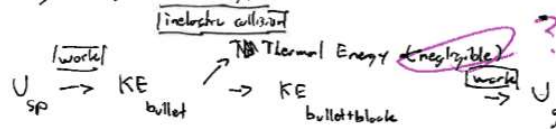
the system was given right once they hit, then using an energy lens again, the KE at that point is equal to the  $U_g$ , as KE is all converted to  $U_g$  since no other energies are present and energy is conserved, and use that to find the change in height.

Energy  
 $U_{sp} = KE_{projectile}$       momentum  
 $\frac{1}{2} k x^2 = \frac{1}{2} m_p v_p^2 \Rightarrow m_p v_p = m_{p+b} v_f \Rightarrow \frac{1}{2} m_{p+b} v_f^2 = m_{p+b} g \Delta h$

distance compressed

Here's the second way... where they went down a wrong direction and then realized it!

Looking through an energy lens because we are analyzing various transformations of energy

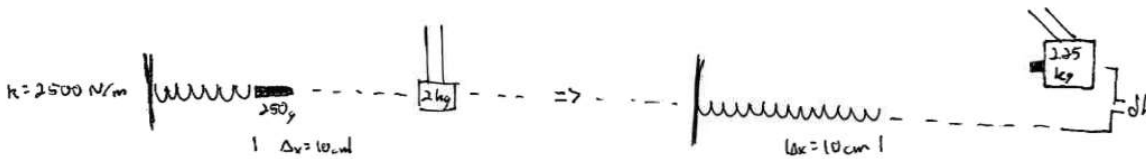


*kinetic energy is conserved in an inelastic collision*

This shows that, neglecting air resistance and thermal energy generated by the collision, no energy is "lost" in the process, thus the spring's elastic potential energy is equal to the block+bullet's gravitational  $U_g$ .

This means I can use this energy lens to calculate  $\Delta h$

*Bad bad bad*



$$U_{sp} = \frac{1}{2} \cdot 2500 \text{ N/m} \cdot (0.1 \text{ m})^2$$

$$= 1250 \text{ N/m} \cdot 0.01 \text{ m}^2 = 12.5 \text{ Nm}$$

$$= 12.5 \text{ J}$$

Since all  $U_{sp}$  was converted to  $U_g$ , eventually,  $U_g$  also is 12.5 J

$$12.5 \text{ J} = 2.25 \text{ kg} \cdot 10 \text{ m/s}^2 \cdot h$$

$$h = \frac{12.5}{2.25} \text{ m} = \left(\frac{5}{9}\right) \text{ m} = \frac{5}{9} \text{ m}$$

Hum I used a momentum lens and I guess proved that you can't actually do what I said, sorry it's small, but if it's worth anything, here

$$12.5 \text{ J} = \frac{1}{2} \cdot 25 \text{ kg} \cdot v^2$$

$$12.5 \text{ J} = \frac{1}{2} \text{ kg} \cdot v^2$$

$$v = 10 \text{ m/s}$$

$$p_{bullet} = 25 \text{ kg} \cdot 10 \text{ m/s} = 25 \text{ kg} \cdot \text{m/s}$$

$$25 \text{ kg} \cdot \text{m/s} = 2.25 \text{ kg} \cdot v$$

momentum conserved in inelastic collision

$$v = \frac{25 \text{ kg} \cdot \text{m/s}}{2.25 \text{ kg}} = \frac{5}{9} \text{ kg} \cdot \text{m/s} \cdot \frac{12}{9} \text{ m/s} = \frac{10}{9} \text{ m/s}$$

$$KE_{block} = \frac{1}{2} \cdot \frac{9}{4} \text{ kg} \cdot \left(\frac{10}{9}\right)^2 \text{ m/s}^2$$

$$= \frac{9}{8} \text{ kg} \cdot \frac{100}{81} \text{ m}^2/\text{s}^2$$

*much much better*

$$\frac{25}{9} \cdot \frac{1}{9} \cdot \frac{1}{10} = \frac{25}{9} \cdot \frac{1}{9} \cdot \frac{1}{10} = \frac{5}{9} \cdot \frac{1}{9} \cdot \frac{1}{10} = \frac{5}{81}$$

$$\frac{25}{18} \text{ J} = 2.25 \text{ kg} \cdot 10 \text{ m/s}^2 \cdot h \parallel h = \left(\frac{5}{9}\right) \text{ m} = \frac{5}{9} \text{ m}$$

